



# DIU Take-Off Programming Contest

Spring 2020

[Main Round]

**Organized By**



## Problem Analysis

**Platform Support**



# Toph

## Judging Panel

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### Special Judge

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**Trainer**

**DIU ACM**

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**10<sup>th</sup> Semester**

**Department of CSE**

**Daffodil International University**

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### Judges

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**Md. Erfanul Islam**

**Nazmus Sakib**

**Riadh Hasan**

**Shimul Shutrathar**

10<sup>th</sup> Semester

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7<sup>th</sup> Semester

7<sup>th</sup> Semester

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## A. Heart of the Demon

**Category:** Pre-Stopper (Data structure)

**Problem Setter:** Ahmed Abdullah Shourav

**Reviewer:** Md. Erfanul Islam, Riadh Hasan

**Special Thanks:** Nazmus Sakib

**Analysis:**

From the problem statement, we know in each step we need to remove the smallest element from the remaining element and stamina will be used is the number of elements on its left.

Or we can say the cost of removing the smallest element is the number of elements on its left which is greater than this. If  $j$  is the index of the smallest element and  $i$  is the index of all the elements greater than this where  $i < j$  then all the pair  $(i, j)$  is called an inversion, so the actual problem is to find the number of inversions in the given array.

Formally, If  $i < j$  and  $ar[i] > ar[j]$  then the pair  $(i, j)$  is called an inversion of the  $ar[]$ .

Total inversion count of an array can be calculated in several approaches,

1. STL Ordered set (PBDS)
2. Binary Indexed Tree (BIT)
3. Segment Tree
4. Merge sort

We will discuss the Merge Sort solution here,

When we merge two sorted arrays, left and right, we must put the element from right into the new, sorted array if it is smaller than the element on the left. In this situation all the elements in the left array are greater than this element on the right side. We can count the number of inversion in this step, which is the count of the remaining element in the left array. Sum of all of these counts is the inversion count of the whole array. The complexity of this solution is the same as the complexity of merge sort  **$O(n \log(n))$** .

And the middle of the array is the median of the array, as  $n$  is always odd the median is  $arr[n/2]$ .

## B. Buy Two, Get One Free

**Category:** if-else

**Problem Setter:** Shah Habibul Imran

**Reviewer:** Rahat Islam Srijon

**Analysis:**

If you observe carefully, you may notice that the sum of any number of even integers is always even. Also, the sum of an even number of odd integers is always even.

Therefore, the sum of two integers will be even only when one of the integers is odd and another is even. So, all you need to check if there is at least one even integer and one odd integer for you to pick.

## C. Treat? Itadakimasu...

**Category:** If-Else+Math

**Problem Setter:** Nazmus Sakib

**Reviewer:** Md. Albin Hossain

**Analysis:**

All we need to do is to find out a number  $n$ , made of the last two digits of multiplication of given four numbers. Then If we divide  $n$  by 25 then we will get which level it belongs to.

Lets say given numbers are  $a, b, c, d$  and  $m = a * b * c * d$ .

It is a fact that If we divide a number by 10 we get the last digit of that number as remainder. And If we divide a number by 100 we get a number consisting of the last two digits of that number as remainder. Thus,  $n = m \% 100$  and  $\text{floor}(n/25)$  is our desired answer.

One drawback of this solution is, we won't be able to store the result of multiplication with int (or even long long int) data type if the given numbers are large enough.

As we know from modular arithmetic,  $(a * b) \% \text{mod}$  is the same as  $((a \% \text{mod}) * (b \% \text{mod})) \% \text{mod}$ .

Thus for this problem we can find the remainder of all four numbers after dividing by 100 and then multiply them. We again divide the result of multiplication to get the last two digits. Thus, we can avoid overflow in the multiplication step and then we determine the level of Katana with the process mentioned above.

So the solution would be:

$\text{floor}((((a \% 100) * (b \% 100) * (c \% 100) * (d \% 100)) \% 100) / 25)$ .

## D. Vaccination in BDesh

**Category:** Loop

**Problem Setter:** Md. Shameem Alam

**Reviewer:** Ahmed Abdullah Shourav

**Special Thanks:** Tanima Hossain, Md.Erfanul Islam

### Analysis:

To solve the problem we need knowledge about how Loop works and some basic arithmetic operations. We need to do the following tasks:

Find each day's spiders who will get fully recovered. And can calculate this using mod(%) operation, i.e  $(a_i \% K)$

Sum all of N day's results we get from doing the task of above.

So, the answer is:  $(a_1 \% K) + (a_2 \% K) + (a_3 \% K) + \dots + (a_n \% K)$

Time Complexity:  $O(T * N)$

## E. Bored in Box

**Category:** Geometry

**Problem Setter:** Md. Albin Hossain

**Reviewer:** Md. Erfanul Islam

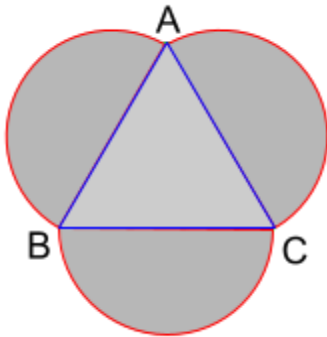
**Special Thanks:** Mahmud Sajjad Abeer

**Analysis:**

If we subtract the area of the circumcircle from the summation of area of triangle and area of the half circles then we can find the area of dark shaded places.

Haven't got yet?..... Let's see in detail.

Here is our triangle with the half circles on its sides. Let us call it *Figure 1*.



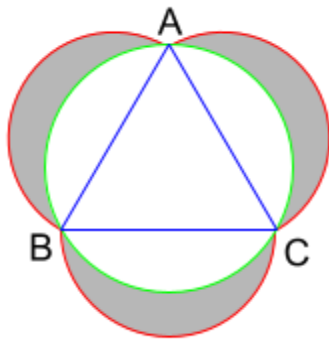
That is,  $Figure\ 1 = Triangle + 3 \times Half\ Circles$

As the triangle is equilateral, the radius of the half circles are also equal.

We have one side of the triangle, AB and we can see that the radius of the *Half Circles* are  $\frac{AB}{2}$ . Using this information we can find the total area of *Figure 1*.

Now if we draw the circumcircle of the triangle we get our final figure.





So, remaining dark region outside of the circumcircle is our desired answer. We can find it by,

$$\text{Dark Region} = \text{Figure 1} - \text{Circumcircle}$$

**N.B:** Formulas to calculate the needed areas are given in the problem statement ([except one](#)).

## F. Tanjiro's Training With Kanao

**Category:** Implementation

**Problem Setter:** Rahat Islam Srijon

**Reviewer:** Nazmus Sakib

**Special Thanks:** Md. Erfanul Islam

### Analysis:

If read carefully, the problem is very clear and straightforward.

You are given two arrays, you have to tell if there are any  $x$  and  $d$  such that  $x$  is the number of skipped elements and  $d$  is the interval between elements in the second array, taking the elements, the differences between elements from the first array and second array stays the same all over.

If we do what is told, for all reasonable  $x$  and  $d$ , we can easily find if there are such  $x$  and  $d$  for which the system holds and the constraints are small enough for that to be done.

We can check for  $x$  and  $d$  using 3 nested loops.

The first one is for all  $x$ ,

The second one is for all  $d$ ,

The third one is for simulating the situation for that  $x$  and  $d$ .

$x$  will be always smaller than  $n-m+1$ , if not it won't be valid because at some point  $x+i*d$  will exceed  $n$ .

$d$  will be always smaller than  $n/(x+(m-1)) < n$ , if not then  $x+i*d$  will exceed  $n$  and become invalid.

And the third loop will iterate over the first array to check differences between respective elements. If all the differences are the same then we can say that we have found such  $x$  and  $d$ . On the other hand, if even after checking for all possible  $x$  and  $d$ , there was no case where the differences were the same we can be sure that there was no such  $x$  and  $d$ .

The overall complexity becomes  $O(n*n*m)$ .

## G. Inosuke and Trailing Zero

**Category:** Number Theory

**Problem Setter:** Shimul Shutrathar

**Reviewer:** Md. Shameem Alam

**Analysis:**

Trailing zeros are created for multiplication of 10. we need to find out how many 10 are multiplied in the  $\frac{resA}{resB}$ .

10 prime factorization is.  $2^1 \times 5^1$

To make 10, powers of 2 and 5 must be 1. For how many 10 are multiplied in a number we figure out by finding 2 and 5 power in its prime factorization. The minimum power of 2 and 5 will be the how many 10 that are multiplied in the number.

We can express division in the following way.

$$\frac{a}{b} = a^1 \times b^{-1}$$

Now

$$\frac{2^{ae2} \times 5^{ae5}}{2^{be2} \times 5^{be5}}$$

$$\Rightarrow 2^{ae2 - be2} \times 5^{ae5 - be5}$$

Minimum of  $(ae2 - be2)$  and  $(ae5 - be5)$  will be trailing zero in  $\frac{a}{b}$ .

**Part - 1:** In this problem you have to find out power of 2 in resA and resB, After that subtract the power of 2 in resB from the power of 2 in resA.

To calculate the power of 2 in A first, prime factorize each element of A and count the total number of 2 in it that is the power of 2 in resA. Do the same for B to calculate the power of 2 in resB.

**Part - 2:** After that find power of 5 in resA and resB in the same way. Now, subtract the power of 5 in resB from the power of 2 in resA.

Minimum of subtraction values from part - 1 and part - 2 is the answer.

## H. Road to MUZAN

**Category:** String

**Problem Setter:** Riadh Hasan

**Reviewer:** Md. Shah Habibul Imran

**Analysis:**

In the palindromic string if we split the string in two parts from the middle we have to maintain the same character on both spilled strings that is why we can use any number of even frequency characters in our longest palindromic string.

Now for odd frequency characters we can use only one odd frequency character. For other odd frequency characters we will decrease the frequency by one and add new frequency in our answer string.

Now we can add all even frequency characters and maximum value of odd frequency characters and decrease the value of other odd frequency characters.

time complexity :  $O(t*(n+q))$

space complexity:  $O(n)$

## I. Here is a treat for You! 🍕🍔

**Category:** Stopper

**Problem Setter:** Tanima Hossain

**Reviewer:** Mahmud Sajjad Abeer, Md. Erfanul Islam, Md. Shah Habibul Imran

**Analysis:**

**Observation:** Number of techniques for each of them depends on the number of techniques they had in the previous meet. So, it becomes a linear recurrence.

**Solution:** If you brute force it, it will surely get a TLE as the complexity for that is  $O(T \times n)$  and as there is no pattern in the recurrences we can solve this problem with **matrix exponentiation**. The complexity of the solution becomes  $O(T \times \log N)$ .

## J. Behold! The Stopper!!!

**Category:** Give away

**Problem Setter:** Md. Erfanul Islam

**Reviewer:** Tanim Hossain

**Analysis:**

```
#include <stdio.h>
int main(){
    printf("Never Give Up!\n");
    return 0;
}
```